

# Search for a massive invisible particle $X^0$ in $B^+ \rightarrow e^+ X^0$ and $B^+ \rightarrow \mu^+ X^0$ decays

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We present a search for a non-Standard-Model invisible particle  $X^0$  in the mass range  $0.1\text{--}1.8\text{ GeV}/c^2$  in  $B^+ \rightarrow e^+ X^0$  and  $B^+ \rightarrow \mu^+ X^0$  decays. The results are obtained from a  $711\text{ fb}^{-1}$  data sample that corresponds to  $772 \times 10^6 B\bar{B}$  pairs, collected at the  $\Upsilon(4S)$  resonance with the Belle detector at the KEKB  $e^+e^-$  collider. One  $B$  meson is fully reconstructed in a hadronic mode to determine the momentum of the lepton of the signal decay in the rest frame of the recoiling partner  $B$  meson. We find no evidence of a signal and set upper limits on the order of  $10^{-6}$ .

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Since their theoretical proposal by Pauli [1] and the discovery by Cowan *et al.* [2], neutrinos have played a crucial role in developing and shaping the standard model (SM) of elementary particle physics. Recent observation of neutrino oscillation [3] requires that they have non-zero masses. But in the minimal SM, there is no mechanism for them to acquire non-zero mass.

Many new physics models beyond the SM introduce heavy neutrinos to explain neutrino masses through the so-called seesaw mechanism [4]. Moreover, these heavy

neutrinos can help explain dark matter in the universe. It is of great interest to search for heavy neutrino-like particles. Such a heavy neutrino is an invisible particle, which we denote  $X^0$ , and can be studied in  $B^+$  decays to  $l^+ X^0$  [5], where  $l$  denotes an electron or muon.

There are further possibilities for the  $X^0$  candidate in hypotheses of new physics beyond the SM. One is sterile neutrinos in large extra dimensions [6] and in the neutrino minimal standard model ( $\nu$ MSM) that incorporate the three light singlet right-handed fermions [7]. Another

option is the lightest supersymmetric particle (LSP) in the minimal supersymmetric standard model (MSSM) [8] assuming  $R$ -parity violation. If the  $X^0$  is the LSP, it can be a neutralino that is produced via the process shown in Fig. 1. If we observe a particle  $X^0$  that is significantly heavier than an SM neutrino, it would indicate new physics.

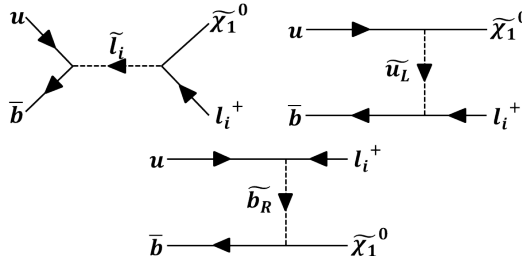


FIG. 1: Some Feynman diagrams to produce the lightest neutralino from  $B$  meson decays in MSSM assuming  $R$ -parity violation.

In this article, we report on searches for  $B^+ \rightarrow e^+ X^0$  and  $B^+ \rightarrow \mu^+ X^0$  decays with an  $X^0$  mass in the range 0.1 to 1.8 GeV/ $c^2$ . The searches use an  $e^+e^- \rightarrow \Upsilon(4S)$  data sample of 711 fb $^{-1}$  containing  $772 \times 10^6 B\bar{B}$  events produced by the KEKB [9] asymmetric  $e^+e^-$  collider at  $\sqrt{s} = 10.58$  GeV, which is at the  $\Upsilon(4S)$  resonance, and recorded with the Belle detector.

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Čerenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters, and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return yoke located outside of the coil is instrumented to detect  $K_L^0$  mesons and to identify muons (KLM). The detector is described in detail elsewhere [10].

We assume the  $X^0$  is invisible and has a lifetime long enough to escape from the Belle detector. Assuming a mean  $X^0$  lifetime of  $10^{-6}$  seconds, fewer than 1% of  $X^0$  decay in the detector. We search for a signal by exploiting the two-body decay kinematics of  $B^+ \rightarrow l^+ X^0$  decays. The magnitude  $p_l^B$  of the momentum of the charged lepton measured in the rest frame of the parent  $B^+$  meson depends on the  $X^0$  mass. The resolution of  $p_l^B$  is affected by the unknown direction of the parent  $B^+$ . To improve this resolution, we fully reconstruct the other  $B$  meson in the event in a hadronic decay mode. For this reconstruction, an algorithm based on hierarchical neural networks [11] is used. The charged  $B$  meson, thus reconstructed with 615 exclusive decay channels, is labeled  $B_{\text{tag}}$  and is used to constrain the kinematics of the signal  $B$  meson. The  $B_{\text{tag}}$  reconstruction quality for each candidate is denoted by a variable  $o_{\text{tag}}$ , which is the output from the neural network algorithm. A  $B_{\text{tag}}$  can-

didate that is reconstructed with complete certainty has  $o_{\text{tag}} = 1$  while one with no certainty has  $o_{\text{tag}} = 0$ .

When there are multiple  $B_{\text{tag}}$  candidates in an event, we choose the candidate that has the largest  $o_{\text{tag}}$  value from the hadronic tagging algorithm. We require  $o_{\text{tag}} > 0.0025$ , for which the purity of the tagged  $B^+$  sample is 73%; this falls to 56% with a random selection of the best  $B_{\text{tag}}$  candidate. To suppress combinatorially formed  $B_{\text{tag}}$  candidates, we further require the following conditions on the energy difference  $\Delta E = E_{B_{\text{tag}}} - \sqrt{s}/2$ , and the beam-energy-constrained mass  $M_{\text{bc}} = \sqrt{(s/4)/c^4 - |\vec{p}_{B_{\text{tag}}}|^2/c^2}$ , where  $\vec{p}_{B_{\text{tag}}}$  and  $E_{B_{\text{tag}}}$  are the reconstructed momentum and energy, respectively, of the  $B_{\text{tag}}$  candidate in the center-of-mass (CM) frame:  $M_{\text{bc}} > 5.27$  GeV/ $c^2$  and  $|\Delta E| < 0.05$  GeV.

The efficiency,  $\epsilon_{\text{tag}}$ , of hadronic  $B$  tagging is initially determined by Monte Carlo (MC) simulation, then corrected for a small data-MC difference by analyzing control sample modes composed of the semileptonic  $B^+ \rightarrow \bar{D}^{(*)0} l^+ \nu_l$  decays. For  $\bar{D}^{(*)0} l^+ \nu_l$ , we consider only the  $\bar{D}^0$  decays to  $K^+ \pi^-$ ,  $K^+ \pi^- \pi^0$ , and  $K^+ \pi^- \pi^+ \pi^-$ . For  $\bar{D}^{*0} l^+ \nu_l$ , we use  $\bar{D}^{*0}$  decays to  $\bar{D}^0 \pi^0$  and  $\bar{D}^0 \gamma$  with  $\bar{D}^0 \rightarrow K^+ \pi^-$ .

We calculate the weighted average of the correction factors determined from each control mode with their branching fractions as weights, as described in Ref. [12]. After the correction, the efficiency of the  $B_{\text{tag}}$  reconstruction is 0.17% for  $B^+ \rightarrow e^+ X^0$  and 0.18% for  $B^+ \rightarrow \mu^+ X^0$ , with the relative uncertainty of  $\epsilon_{\text{tag}}$  being 6.4% [13].

After removing particles used in the  $B_{\text{tag}}$  reconstruction, we require that an event have only one charged track, that its charge be opposite that of the  $B_{\text{tag}}$  and that its laboratory-frame momentum exceed 1.0 GeV/ $c$ . This charged track is required to satisfy  $|dz| < 2.0$  cm and  $dr < 0.5$  cm, where  $|dz|$  and  $dr$  are the distances of closest approach to the interaction point along and perpendicular to the beam axis.

We require that this charged track be identified as an electron or a muon. Electrons are identified by means of a likelihood ratio based on the following information: the ratio between the cluster energy in the ECL and the track momentum from the CDC ( $E/p$ ), the specific ionization  $dE/dx$  in the CDC, the position and shower shape of the cluster in the ECL and the response from the ACC. Muon identification uses the matching information between the charged track and the KLM-hit positions as well as the KLM penetration depth. With our track selection criteria, the electron and muon efficiencies are over 90% and their hadron misidentification rates are below 0.5% and 5%, respectively. A more detailed description of the lepton identification can be found in Ref. [14].

The continuum background events ( $e^+e^- \rightarrow q\bar{q}$  with  $q = u, d, s, \text{ or } c$ ) are suppressed using the event shape difference between  $B\bar{B}$  and continuum events. In the CM frame, due to the low momentum of the  $B$  mesons, the event shape of a  $B\bar{B}$  event tends to be more spherical while the continuum backgrounds tend to be more

jet-like. To exploit this difference, we use the cosine of the thrust angle,  $\cos\theta_T$ , to suppress the continuum backgrounds. Here,  $\theta_T$  is the angle between the thrust axis of the  $B_{\text{tag}}$  and the momentum of the signal-side lepton in the CM frame; the thrust axis is the direction that maximizes the sum of the longitudinal momenta of the particles. We apply  $|\cos\theta_T| < 0.9$  and  $|\cos\theta_T| < 0.8$  for electron and muon candidates, relatively. The more stringent condition is used for the muon due to its larger misidentification probability.

The remaining backgrounds, especially those with extra neutral particles from the signal  $B$  meson side, are suppressed by using the variable  $E_{\text{ECL}}$ , which is defined as the sum of the extra energy in the ECL beyond that associated with the  $B_{\text{tag}}$  constituents and the signal-side lepton. In calculating  $E_{\text{ECL}}$ , we consider only clusters with energies above 50 MeV in the barrel, 100 MeV in the forward endcap, and 150 MeV in the backward endcap [10]. The higher thresholds in the endcap regions reflect the more severe beam background in those regions. We require  $E_{\text{ECL}} < 0.5$  GeV to enhance the signal.

We determine the signal yield using a fit to the  $p_l^B$  distribution. Figure 2 shows the MC expectation for signal and background for  $p_l^B$  between 1.8 GeV/c and 2.8 GeV/c. The background level becomes increasingly significant as  $p_l^B$  falls below 2.3 GeV/c.

As a result, we restrict our search to  $M_{X^0} \leq 1.8$  GeV/ $c^2$ , beyond which the search sensitivity is greatly degraded due to background. For each assumed value of  $M_{X^0}$ , the  $p_l^B$  signal region is optimized based on the expected upper limit of the signal branching fraction, which is estimated by MC simulation. Considering the width of the so optimized signal regions of  $p_l^B$  in Table I, we perform the search in 0.1 GeV/ $c^2$  steps of  $M_{X^0}$ , whereby the entire test region ( $0.1$  GeV/ $c^2 \leq M_{X^0} \leq 1.8$  GeV/ $c^2$ ) is covered without any gaps.

The number of expected background events in the  $p_l^B$  signal region is estimated by first performing a maximum likelihood fit to  $p_l^B$  in the region  $1.8$  GeV/c <  $p_l^B$  < 2.25 GeV/c (“sideband”), where we expect very little contribution from the signal events for  $M_{X^0} < 1.8$  GeV/ $c^2$ . The fitted yield is then extrapolated to the  $p_l^B$  signal region, which is discussed in more detail below. To fit the  $p_l^B$  sideband, we consider the following sources of background: continuum,  $b \rightarrow c$  decays, semileptonic  $b \rightarrow ul\nu$  decays, and other rare and leptonic  $B$ -decay processes. The background distributions are modelled by the probability density functions (PDFs), which are described in Table II. We do not consider continuum background in the fitting because it is almost completely removed by our pre-selection. Note that we utilize separate PDFs for the  $B^+ \rightarrow l^+\nu_l\gamma$ ,  $B^+ \rightarrow \pi^0 l^+\nu_l$ , and  $B^+ \rightarrow \pi^+ K^0$  decays, as these modes show peaking behavior in the  $p_l^B$  distribution. The  $B^+ \rightarrow l^+\nu_l\gamma$  modes (excluding taus), which have not been observed, could produce a substantial yield of high-momentum leptons near the signal regions, so we simulate them with dedicated large-sample-size MC. We use a branching fraction

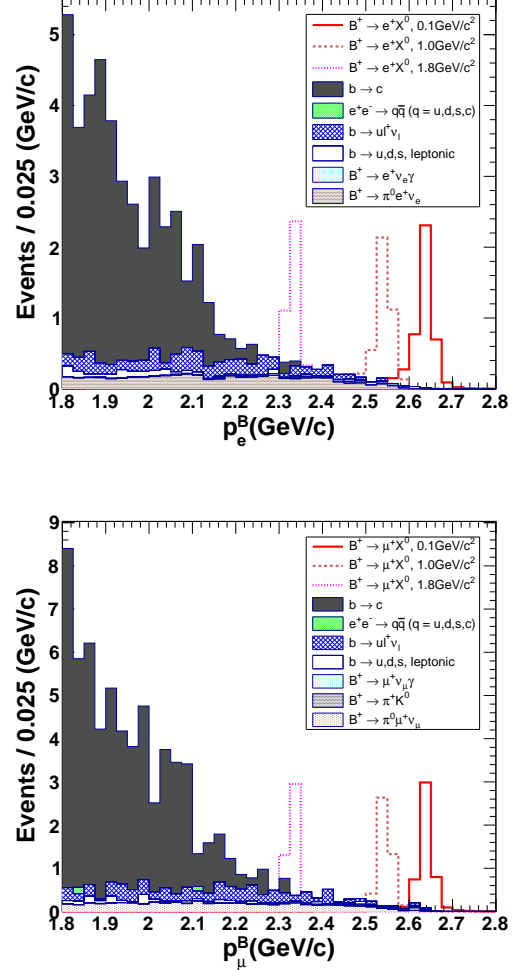


FIG. 2:  $p_l^B$  MC distributions for  $B^+ \rightarrow e^+ X^0$  (top) and  $B^+ \rightarrow \mu^+ X^0$  (bottom), where signal MC is arbitrary scaled. The  $e^+ e^- \rightarrow q\bar{q}$  background is negligible.  $B^+ \rightarrow e^+ \nu_e \gamma$ ,  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$  and  $B^+ \rightarrow \pi^+ K^0$  backgrounds become important for  $p_l^B > 2.5$  GeV/c.

of  $2 \times 10^{-6}$  for  $B^+ \rightarrow e^+ \nu_e \gamma$  and  $B^+ \rightarrow \mu^+ \nu_\mu \gamma$ , which is lower than the recently measured upper limit [15]. For  $B^+ \rightarrow \pi^0 l^+ \nu_l$ ,  $B^+ \rightarrow \pi^+ K^0$  and  $B^+ \rightarrow l^+ \nu_l \gamma$ , high-statistics MC samples are produced with 300, 500, and 2500 times, respectively, more integrated luminosity than the data. In the fit, only the overall normalization is free and the relative yields of all background modes are fixed based on the measured or assumed branching fractions. Finally, the number of background events extrapolated in each signal region is corrected by the data-MC difference. The correction factor is calculated as the ratio of the number of events in the corresponding  $p_l^B$  signal region in the  $E_{\text{ECL}}$  sideband ( $1.8$  GeV/c <  $p_l^B$  < 3.0 GeV/c,  $0.5$  GeV <  $E_{\text{ECL}}$  < 2.0 GeV) in data and in the MC sample. The range of correction factors is 1.10 - 1.11 for the electron mode and 0.93 - 0.99 for the muon mode.

TABLE I: Summary of upper limits at the 90% CL.

$M_{X^0}$	$p_l^B$ selection (GeV/c)	$\epsilon_s$ [%]	$N_{\text{obs}}$	$N_{\text{exp}}^{\text{bkg}}$	$\mathcal{B}^{90}$
$B^+ \rightarrow e^+ X^0$ for $M_{X^0}$					
0.1 GeV/c <sup>2</sup>	2.52-2.70	0.11	0	$0.36 \pm 0.13$	$< 2.4 \times 10^{-6}$
0.2	2.52-2.70	0.11	0	$0.36 \pm 0.13$	$< 2.4 \times 10^{-6}$
0.3	2.55-2.68	0.11	0	$0.21 \pm 0.13$	$< 2.6 \times 10^{-6}$
0.4	2.55-2.68	0.11	0	$0.21 \pm 0.08$	$< 2.7 \times 10^{-6}$
0.5	2.52-2.70	0.11	0	$0.36 \pm 0.08$	$< 2.5 \times 10^{-6}$
0.6	2.52-2.70	0.11	0	$0.36 \pm 0.13$	$< 2.5 \times 10^{-6}$
0.7	2.52-2.70	0.11	0	$0.36 \pm 0.13$	$< 2.4 \times 10^{-6}$
0.8	2.51-2.62	0.11	0	$0.37 \pm 0.12$	$< 2.5 \times 10^{-6}$
0.9	2.51-2.62	0.10	0	$0.37 \pm 0.12$	$< 2.6 \times 10^{-6}$
1.0	2.51-2.62	0.096	0	$0.37 \pm 0.12$	$< 2.8 \times 10^{-6}$
1.1	2.47-2.57	0.099	0	$0.58 \pm 0.18$	$< 2.4 \times 10^{-6}$
1.2	2.45-2.53	0.096	0	$0.61 \pm 0.19$	$< 2.5 \times 10^{-6}$
1.3	2.43-2.51	0.098	0	$0.72 \pm 0.22$	$< 2.3 \times 10^{-6}$
1.4	2.41-2.51	0.10	0	$0.97 \pm 0.30$	$< 2.0 \times 10^{-6}$
1.5	2.39-2.46	0.093	1	$0.85 \pm 0.27$	$< 4.8 \times 10^{-6}$
1.6	2.37-2.43	0.092	1	$0.84 \pm 0.27$	$< 4.9 \times 10^{-6}$
1.7	2.34-2.39	0.088	1	$0.85 \pm 0.28$	$< 5.1 \times 10^{-6}$
1.8	2.31-2.36	0.087	2	$1.01 \pm 0.34$	$< 7.1 \times 10^{-6}$
$B^+ \rightarrow \mu^+ X^0$ for $M_{X^0}$					
0.1	2.58-2.68	0.12	1	$0.37 \pm 0.14$	$< 4.3 \times 10^{-6}$
0.2	2.58-2.68	0.12	1	$0.37 \pm 0.14$	$< 4.2 \times 10^{-6}$
0.3	2.58-2.68	0.12	1	$0.37 \pm 0.14$	$< 4.3 \times 10^{-6}$
0.4	2.58-2.68	0.12	1	$0.37 \pm 0.14$	$< 4.3 \times 10^{-6}$
0.5	2.58-2.68	0.11	1	$0.37 \pm 0.14$	$< 4.4 \times 10^{-6}$
0.6	2.58-2.68	0.11	1	$0.37 \pm 0.14$	$< 4.6 \times 10^{-6}$
0.7	2.56-2.63	0.11	0	$0.39 \pm 0.13$	$< 2.4 \times 10^{-6}$
0.8	2.54-2.61	0.11	1	$0.41 \pm 0.15$	$< 4.4 \times 10^{-6}$
0.9	2.52-2.60	0.11	1	$0.52 \pm 0.18$	$< 4.3 \times 10^{-6}$
1.0	2.49-2.58	0.11	1	$0.74 \pm 0.25$	$< 4.1 \times 10^{-6}$
1.1	2.49-2.58	0.12	1	$0.74 \pm 0.25$	$< 3.9 \times 10^{-6}$
1.2	2.48-2.53	0.10	0	$0.54 \pm 0.17$	$< 2.4 \times 10^{-6}$
1.3	2.45-2.50	0.10	0	$0.67 \pm 0.21$	$< 2.3 \times 10^{-6}$
1.4	2.42-2.48	0.11	2	$0.90 \pm 0.28$	$< 5.8 \times 10^{-6}$
1.5	2.40-2.47	0.11	5	$1.12 \pm 0.35$	$< 10.6 \times 10^{-6}$
1.6	2.37-2.42	0.10	4	$0.95 \pm 0.30$	$< 9.6 \times 10^{-6}$
1.7	2.34-2.39	0.10	1	$1.09 \pm 0.34$	$< 4.0 \times 10^{-6}$
1.8	2.31-2.37	0.11	1	$1.49 \pm 0.46$	$< 3.3 \times 10^{-6}$

TABLE II: Fit functions for background modes.

Background	$B^+ \rightarrow e^+ X^0$	$B^+ \rightarrow \mu^+ X^0$
$b \rightarrow c$	Gaussian	Gaussian
$b \rightarrow ul\nu_l$	Asymmetric Gaussian	Gaussian
$b \rightarrow u, d, s, \text{leptonic}$	Exponential	Exponential + ARGUS [16]
$B^+ \rightarrow l\nu_l \gamma$	Asymmetric Gaussian	Asymmetric Gaussian
$B^+ \rightarrow \pi^0 l\nu_l$	Asymmetric Gaussian + Gaussian	Asymmetric Gaussian + Gaussian
$B^+ \rightarrow \pi^+ K^0$		Gaussian + Gaussian

The signal branching fractions are obtained by the following equation:

$$\mathcal{B}(B^+ \rightarrow l^+ X^0) = \frac{N_{\text{obs}} - N_{\text{exp}}^{\text{bkg}}}{2 \cdot \epsilon_s \cdot N_{B^+ B^-}}, \quad (1)$$

where  $N_{\text{obs}}$  and  $N_{\text{exp}}^{\text{bkg}}$  are the numbers of observed and

expected background events in the signal region,  $\epsilon_s$  is the signal efficiency, and  $N_{B^+ B^-}$  is the number of  $B^+ B^-$  events.

To evaluate  $\epsilon_s$ , signal MC samples are generated using EvtGen [17], including final-state radiation using PHOTOS [18]. These samples are processed with a detector simulation based on GEANT3 [19]. The signal efficien-

cies are summarized in Table I.

Figure 3 shows the  $p_l^B$  distribution of the on-resonance data. The fitted yield of background in the  $p_l^B$  sideband of on-resonance data is extrapolated to the signal region. The extrapolation factor is determined from background MC samples.

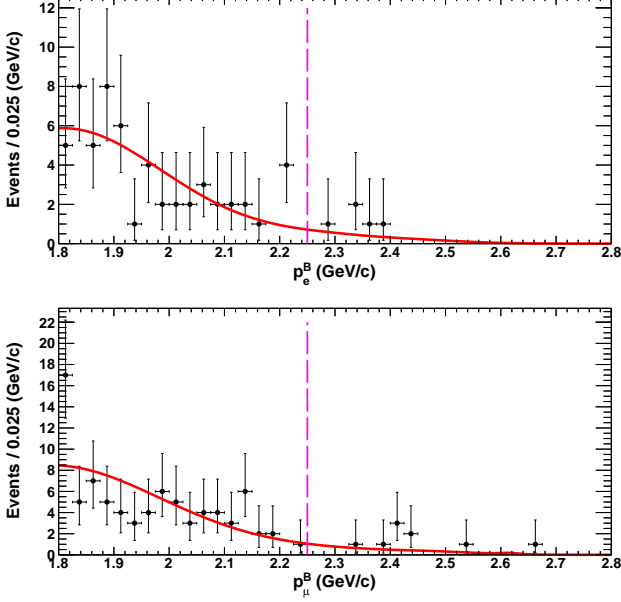


FIG. 3:  $p_l^B$  data distributions for  $B^+ \rightarrow e^+ X^0$  (top) and  $B^+ \rightarrow \mu^+ X^0$  (bottom), where the red curve indicates the background expectation and the magenta dashed line indicates the upper bound of the  $p_l^B$  sideband.

The observed yields in the signal region are summarized in Table I. There is no signal excess for either mode in any  $M_{X^0}$  range. In the muon mode for  $M_{X^0} = 1.5 \text{ GeV}/c^2$  ( $1.6 \text{ GeV}/c^2$ ), we find 5 (4) events in the  $p_l^B$  signal region while we expect  $1.12 \pm 0.34$  ( $0.95 \pm 0.29$ ) background events. The local  $p$ -value of this yield, assuming a background-only hypothesis, is 0.60% (1.59%). We obtain the 90% confidence level (CL) upper limit of the signal yield in each case by using the frequentist approach [20] implemented in the POLE (Poissonian limit estimator) program [21], where the systematic uncertainties are taken into account.

The systematic uncertainty consists of the multiplicative uncertainty on  $\epsilon_s \cdot N_{B^+B^-}$  and the additive uncertainty on the background. The multiplicative uncertainty is calculated from the uncertainties on the number of  $B^+B^-$  events, track finding and lepton identification for the signal lepton, the  $\epsilon_{\text{tag}}$  correction, the  $p_l^B$  shape, and the signal MC sample size.

A 1.8% uncertainty is assigned for the uncertainty on the number of  $B$  mesons and the branching fraction of  $\Upsilon(4S) \rightarrow B^+B^-$  [22]. The track-finding uncertainty is estimated by comparing the track-finding efficiency in data and MC, determining it in both cases from the

number of pions in the partially and fully reconstructed  $D^* \rightarrow \pi D^0$ ,  $D^0 \rightarrow \pi\pi K_S^0$ ,  $K_S^0 \rightarrow \pi\pi$  decay chain. For the  $p_l^B$  shape uncertainty, we use the 3.6% uncertainty from the  $B^+ \rightarrow \bar{D}^0 \pi^+$  control sample study in the  $B^+ \rightarrow l^+ \nu_l$  search [13] due to its similar kinematics. The lepton identification uncertainty is estimated by comparing the efficiency difference between data and MC using  $\gamma\gamma \rightarrow l^+ l^-$ . The multiplicative systematic uncertainties are summarized in Table III.

TABLE III: Summary of multiplicative systematic uncertainties on  $\epsilon_s \cdot N_{B^+B^-}$ . The lepton identification and MC statistical uncertainties depend on  $M_{X^0}$  and are given as ranges.

Source	$B^+ \rightarrow e^+ X^0$	$B^+ \rightarrow \mu^+ X^0$
$N_{B^+B^-}$	1.8%	1.8%
Tracking	0.35%	0.35%
$\epsilon_{\text{tag}}$ correction	6.4%	6.4%
$p_l^B$ shape	3.6%	3.6%
Lepton ID	(1.0–1.1)%	(0.8–0.9)%
MC sample size	(1.8–2.0)%	(1.8–1.9)%
Total	7.9%	7.8%

The systematic uncertainties on the background estimation are determined by considering the following sources: uncertainties in the background PDF parameters, the branching fraction of the background modes and the statistical uncertainty from the  $p_l^B$  sideband. Each source is varied one at a time by its uncertainty ( $\pm 1\sigma$ ) and the resulting deviations from the nominal background yield are added in quadrature. For the branching fraction uncertainties of the background modes, we use the world-average values in Ref. [22] for  $B^+ \rightarrow \pi^0 l^+ \nu_l$  and  $B^+ \rightarrow \pi^+ K^0$ . For  $B^+ \rightarrow l^+ \nu_l \gamma$ , a variation of  $\pm 50\%$  is applied. For other modes, where an estimate of the background level is not clearly available, a conservative branching fraction uncertainty of  $^{+100}_{-50}\%$  is assumed.

More than 95% of  $b \rightarrow c$  decays result in observed  $D^{(*)} l^+ \nu_l$  final states, so we use their branching fraction uncertainties [22]. The values of  $N_{\text{exp}}^{\text{bkg}}$  and their uncertainties for both  $B^+ \rightarrow e^+ X^0$  and  $B^+ \rightarrow \mu^+ X^0$  are listed in Table I.

Figure 4 shows the expected number of background events in the signal region as well as the obtained 90% CL upper limits of  $\mathcal{B}(B^+ \rightarrow l^+ X^0)$  for each assumed value of  $M_{X^0}$ . Table I summarizes the  $p_l^B$  signal region, estimated background, signal efficiency, number of observed events, and upper limit of the branching fraction at 90% CL for each assumed value of  $M_{X^0}$  for both modes.

From the branching fraction upper limits, assuming  $R$ -parity violation, we can set bounds on the MSSM-related parameter  $\xi_l$

$$\begin{aligned} \xi_l &= \lambda_{l13}^2 \left( \frac{1}{2M_l^2} + \frac{1}{12M_{u_L}^2} + \frac{1}{6M_{b_R}^2} \right)^2 \\ &= \frac{8\pi(m_u + m_b)^2 \mathcal{B}(B^+ \rightarrow l^+ X^0)}{\tau_{B^+} g'^2 f_B^2 m_{B^+}^2 p_l^B (m_{B^+}^2 - m_l^2 - m_{X^0}^2)} \end{aligned} \quad (2)$$

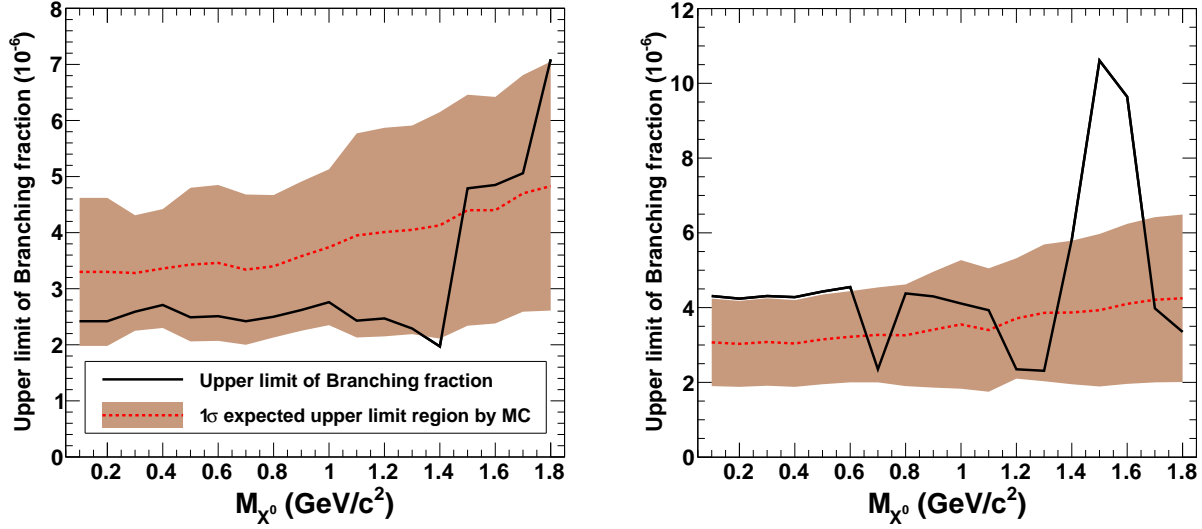


FIG. 4: The branching fraction upper limit as a function of  $M_{X^0}$  and expected upper limit with  $1\sigma$  band;  $e$  mode (left) and  $\mu$  mode (right).

where  $\lambda'$  is a dimensionless  $R$ -parity-violating coupling constant,  $g'$  the weak coupling constant,  $f_B$  the decay constant of the  $B^+$  meson,  $m_{B^+}$  its mass,  $p_l^B$  the momentum of the  $l^+$  in the  $B$  rest frame,  $m_u$  and  $m_b$  the up and bottom quark mass,  $m_l$  the charged lepton mass,  $m_{X^0}$  the neutralino mass, and  $M_{\tilde{f}}$  the sfermion mass that appears as an intermediate particle. The range of upper bounds of  $\xi_e$  is  $4.1 \times 10^{-14}$  to  $1.7 \times 10^{-13} \text{ GeV}^{-4} c^8$  and on  $\xi_\mu$  is  $4.2 \times 10^{-14}$  to  $2.3 \times 10^{-13} \text{ GeV}^{-4} c^8$ .

In summary, we obtain first upper limits for the branching fraction of  $B^+ \rightarrow e^+ X^0$  and  $B^+ \rightarrow \mu^+ X^0$  for an  $X^0$  mass range  $0.1 \text{ GeV}/c^2$  to  $1.8 \text{ GeV}/c^2$  using Belle's full data set, where  $X^0$  is assumed to leave no experimental signature. For 18 assumed values of  $M_{X^0}$  for both modes, upper limits of branching fraction are found to be  $O(10^{-6})$ .

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